

Impact of Momentum Resolution on $\text{BR}(h \rightarrow \mu^+ \mu^-)$ Measurement

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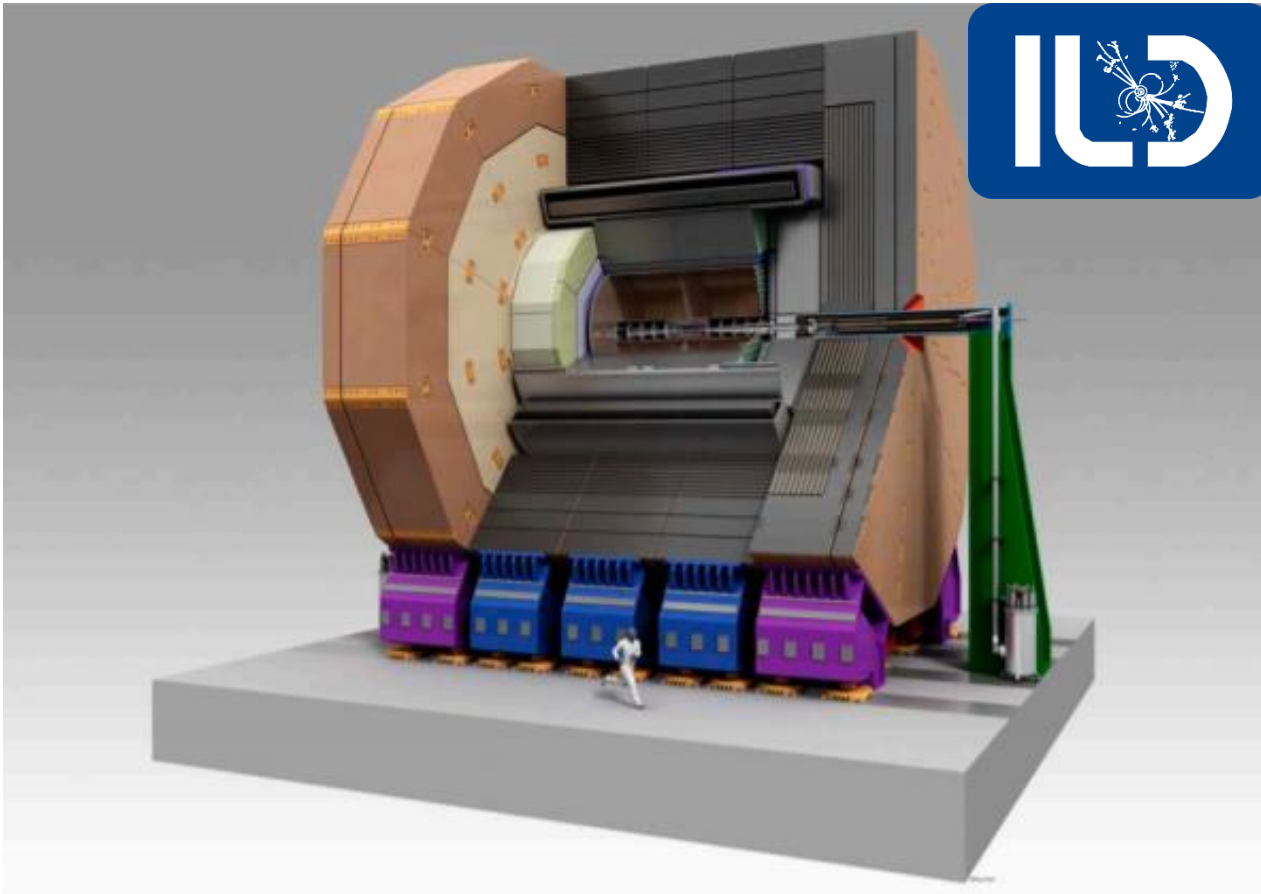
2018/February/22

ILD Meeting @ Ichinoseki



Detector Concept at the ILC

ILD (International Large Detector)



Tracker: Vertex, TPC

Calorimeter: ECAL, HCAL

3.5T magnetic field

Yoke for muon, Forward system

Requirements:

➤ Impact parameter resolution

$$\sigma_{r\phi} < 5 \oplus \frac{10}{p \sin^{3/2} \theta} \mu\text{m}$$

➤ **Momentum resolution**

$$\sigma_{1/p_T} < 2 \cdot 10^{-5} \text{ GeV}^{-1}$$

➤ Energy resolution

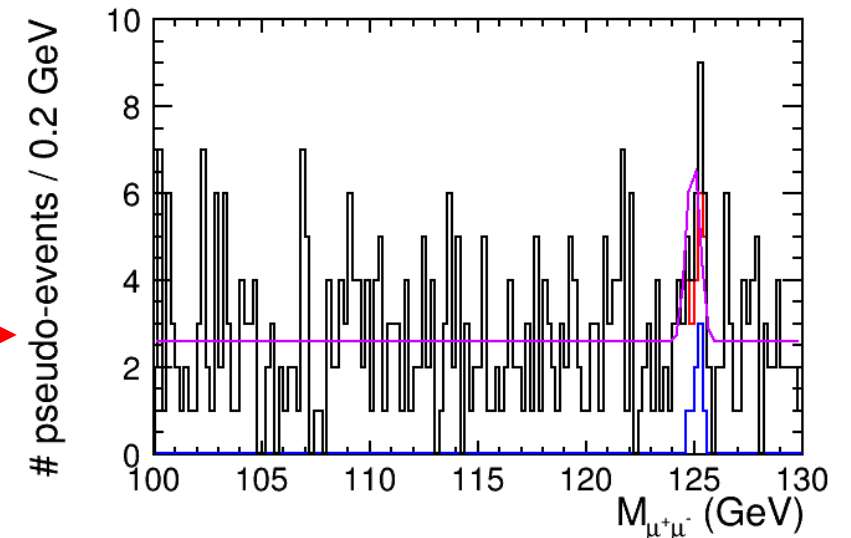
$$\sigma_E/E = 3 - 4\%$$

This Talk: $h \rightarrow \mu^+ \mu^-$

- Challenging analysis: tiny branching ratio ($\text{BR}(h \rightarrow \mu^+ \mu^-) = 2.2 \cdot 10^{-4}$ at $M_h = 125 \text{ GeV}$)
- Can be used for testing:
 - $y_f \propto m_f$
 - mass generation mechanism between 2nd/3rd leptons (κ_μ/κ_τ) and 2nd lepton/quark (κ_μ/κ_c)
- HL-LHC prospects (3000 fb^{-1}): $\sim 21\%$ (ATLAS), $\sim 10\%$ (CMS) for cross section times branching ratio $\frac{\Delta(\sigma \times \text{BR})}{(\sigma \times \text{BR})}$
- Good benchmark process for detector optimization

Brief Summary of Analysis

- Geant4-based full detector simulation with ILD model
- DBD-style MC samples
- Included all possible SM backgrounds
 1. Select $h \rightarrow \mu^+ \mu^-$ candidate using IsolatedLeptonTagger
 2. Channel-specific analysis
 - jet clustering, overlay removal...
 3. Multivariate analysis
 4. Toy MC using $M_{\mu^+ \mu^-}$ distribution



Results

250 GeV	qqh	nnh	500 GeV	qqh	nnh
L	32.5%	108.6%	L	44.5%	37.0%
R	28.1%	110.4%	R	49.5%	74.5%

ILC250 combined = 20.5% (“theoretical limit” = 10.4%)

ILC250+500 combined = **15.4%** (“theoretical limit” = 7.1%)

HL-LHC: 10-21%

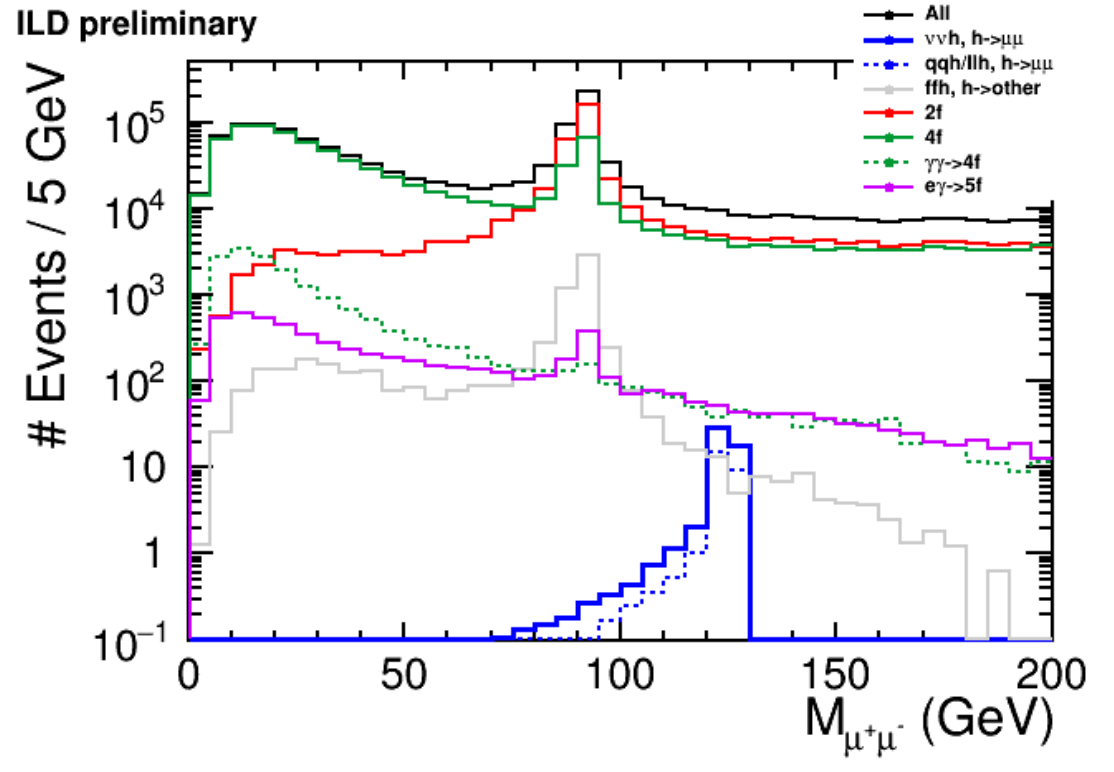
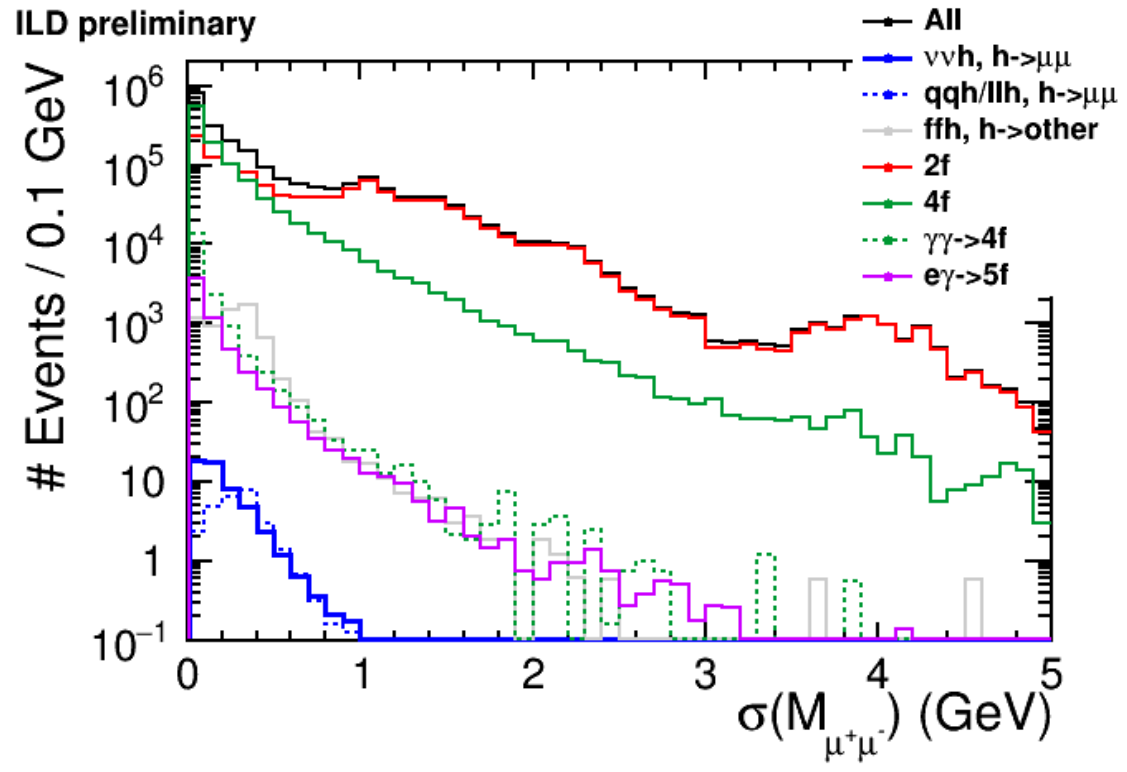
now working on further improvements...

Impact of Momentum Resolution

- In this analysis, the **momentum resolution (P_t resolution)** is most important.
 - For high P_t muons
 - This affects $M_{\mu^+\mu^-}$ which is most important variable for physics analysis.

■ signal

other colors: SM background
plots from nnh500-L



Impact of Momentum Resolution

- Studied what happens when we change momentum resolution artificially
 - 6 benchmark numbers
 - Smearred MCParticle momentum of isolated muon
 - Gaussian-smearred with **constant number**
 - no angular effects, no momentum dependencies

Resolution
(GeV⁻¹)

1 * 10⁻³

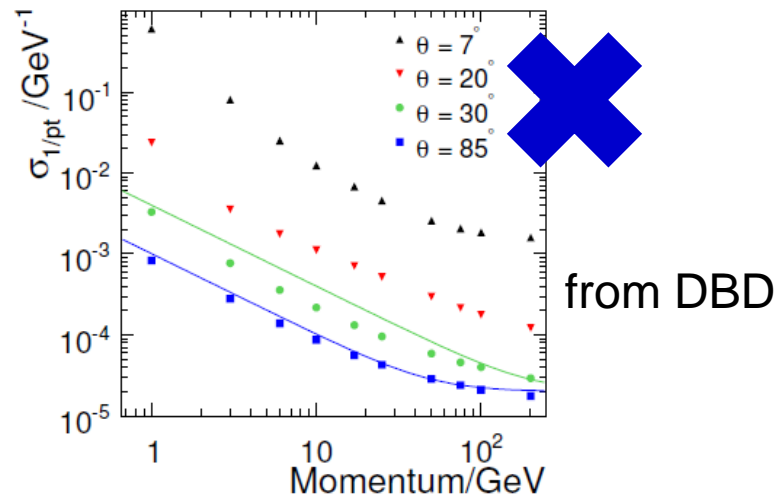
5 * 10⁻⁴

1 * 10⁻⁴

5 * 10⁻⁵

2 * 10⁻⁵

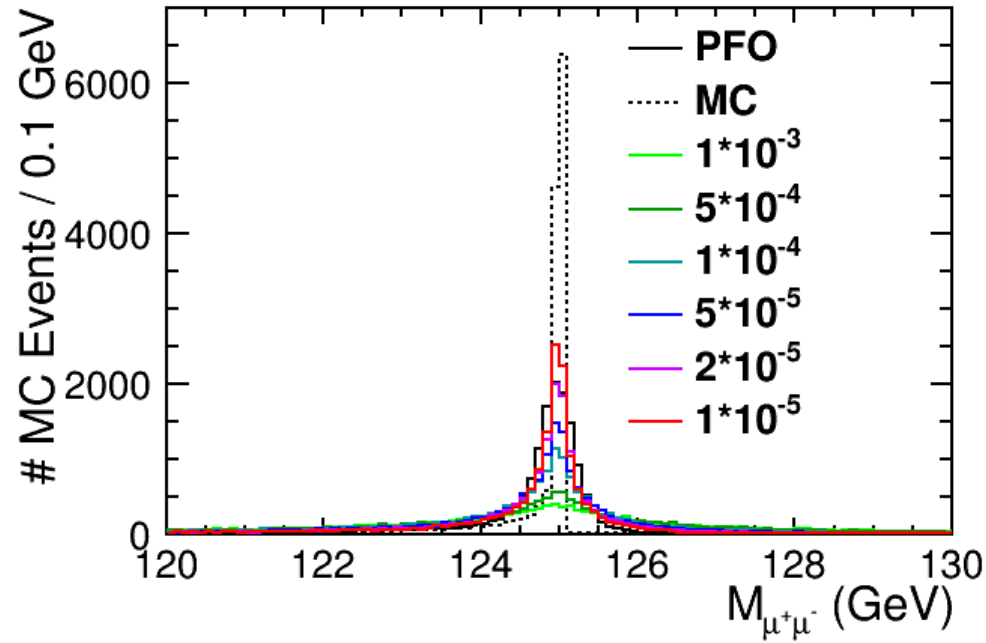
1 * 10⁻⁵



$M_{\mu^+\mu^-}$ Spectrum

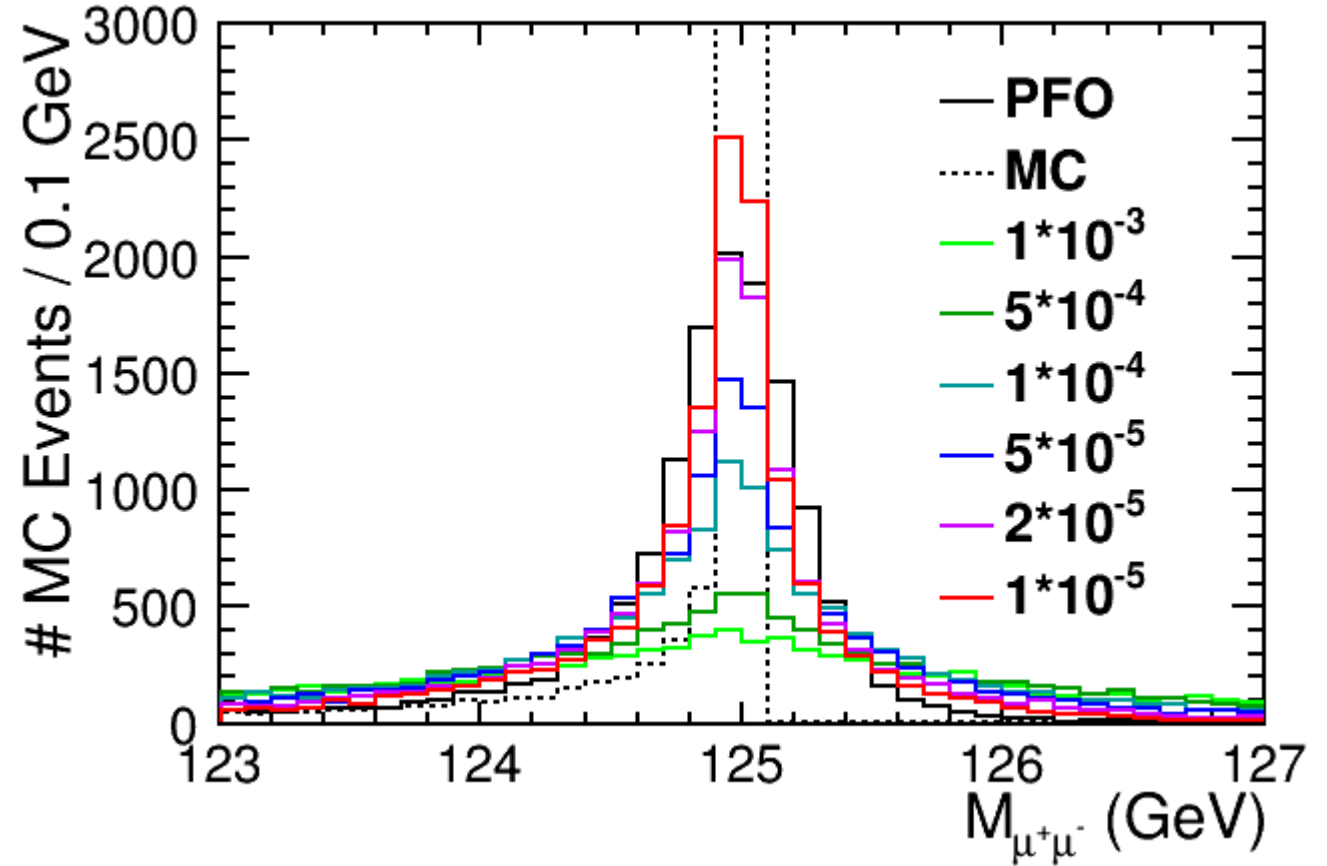
overview

Effect of mometum resolution



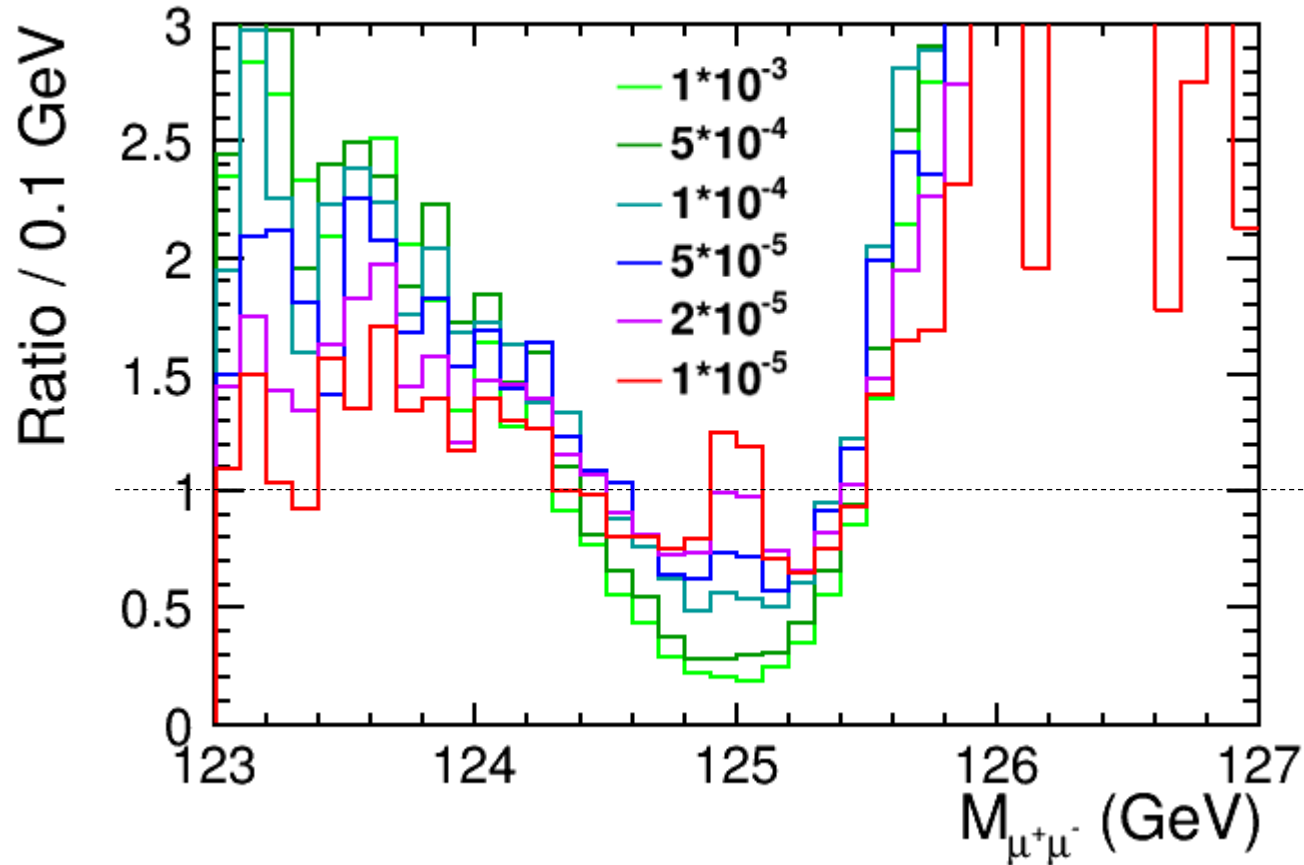
zoom up

Effect of mometum resolution



Ratio Spectrum

Effect of momentum resolution



$$\text{Ratio} \equiv \frac{\text{smeared histogram}}{\text{PFO histogram}}$$

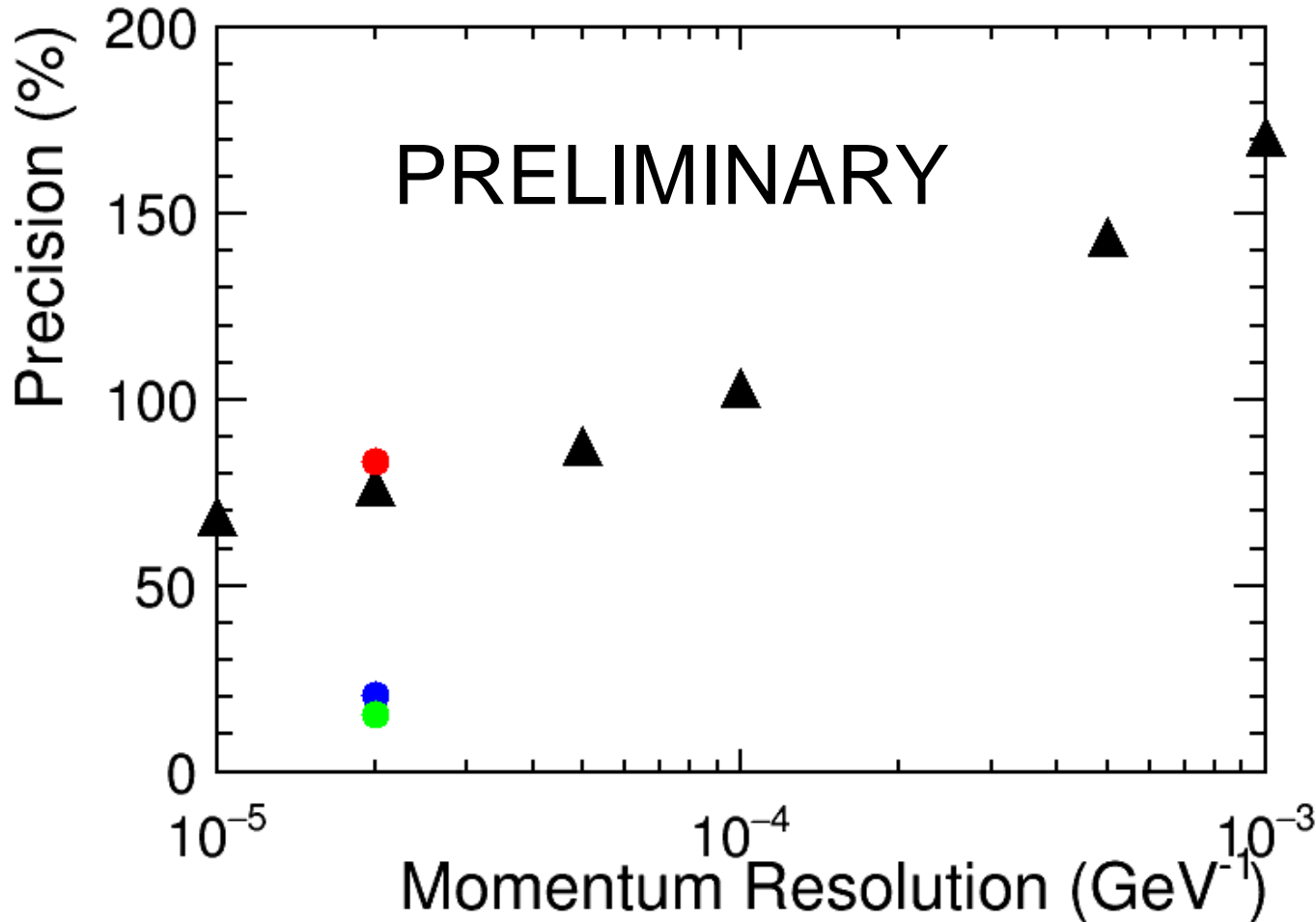
**Clearly worse in
bad momentum resolutions**

Impact to Final Numbers

- It was only for $M_{\mu^+\mu^-}$, but in the end we are interested in the final precision numbers. $\frac{\Delta(\sigma \times \text{BR})}{(\sigma \times \text{BR})}$
- Studied final precision for various momentum resolution
 - Again 6 benchmark numbers (p8)
 - Just changed from $M_{\mu^+\mu^-}$ to $M_{\mu^+\mu^-}^{\text{smear}}$ in toy MC
 - **Studied only for nnh250-L**, due to time limitation (and system problem)
 - clean channel: 2 muons + nothing, small $\gamma\gamma \rightarrow$ hadrons
 - new precuts are applied, pseudomass included in TMVA



Impact to Final Numbers (nnh250-L)



red: full analysis result 83.2%
black: benchmark points
(2*10⁻⁵: 76.9%)
blue: ILC250 20.5%
green: ILC250+500 15.4%

At 2*10⁻⁵:
black is ~10% better than red
angle/momentum dependencies?

Example:
1*10⁻⁴ ---> 2*10⁻⁵: ~25% improvement

Another Study: 1.4 TeV CLIC $h \rightarrow \mu^+ \mu^-$

Eur. Phys. J. C (2015) 75:515

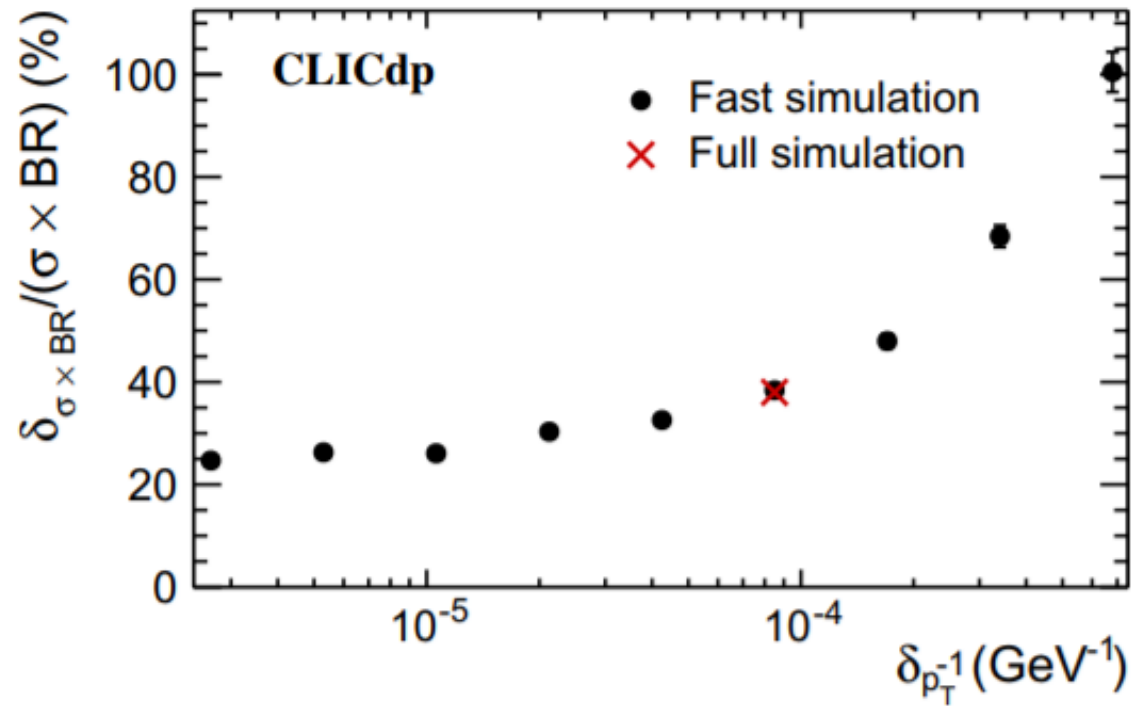


Fig. 11 Dependence of the relative statistical uncertainty of the $\sigma(H\nu\bar{\nu}) \times BR(H \rightarrow \mu^+ \mu^-)$ on the transverse momentum resolution, δ_{1/p_T} , averaged over the signal sample in the whole detector

From paper:

To estimate the benefit of a better p_T resolution, the analysis was repeated by substituting the muon four-momenta reconstructed in the full simulation of the signal by the four-momenta obtained by a parametrisation of the momentum resolution for several different values of the detector resolution.

Full: 38%

- Similar tendency with us
- Performance will saturate around $1 \cdot 10^{-5}$ (~25%)

Summary & Plan

- Studied for impact of momentum resolution in $\text{BR}(h \rightarrow \mu^+ \mu^-)$ measurement
 - similar tendency with CLIC, but saturation is not observed currently
- study more benchmark points and other channels
- work for further improvement and write a paper

BACKUP

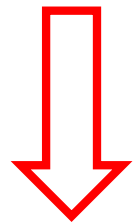


Introduction

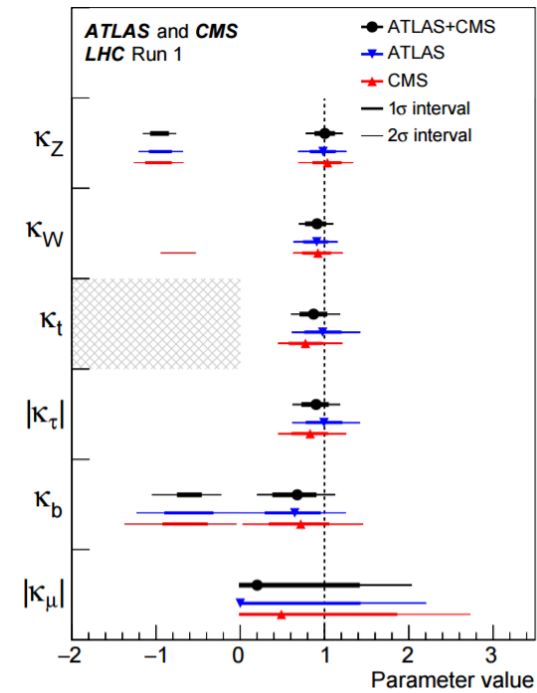
Discovery of Higgs-like boson at the LHC
--> Last particle of SM? Or beyond SM?

Goal: **model-independent** determination of
EWSB sector with **precise** measurements

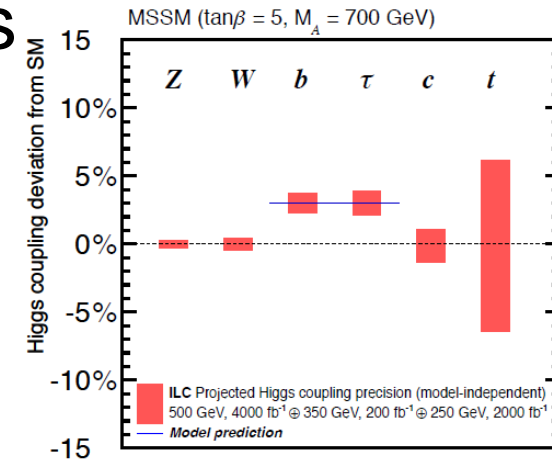
- mass-coupling relation
- any deviation shows the existence of BSM



ILC



JHEP 08
(2016) 045



arXiv:
1506.05992
[hep-ex]

Previous Studies

Everything performed at ≥ 1 TeV, or not realistic

Reference	E_{CM}	beam pol. $P(e^-, e^+)$	$\int L dt$	$\frac{\Delta(\sigma \times \text{BR})}{(\sigma \times \text{BR})}$	comment
LC-REP-2013-006	1 TeV	(-0.8, +0.2)	500 fb ⁻¹	44%	ILC/ILD
arXiv:1306.6329 [hep-ex]	1 TeV	(-0.8, +0.2)	1000 fb ⁻¹	32%	ILC/SiD
arXiv:1603.04718 [hep-ex]	1 TeV	(-0.8, +0.2)	500 fb ⁻¹	36%	ILC/ILD used TMVA
Eur. Phys. J. C73 (2), 2290 (2013)	3 TeV	unpol.	2000 fb ⁻¹	15%	CLIC_SiD $M_h = 120$ GeV used TMVA
Eur. Phys. J. C75 , 515 (2015)	1.4 TeV	unpol.	1500 fb ⁻¹	38%	CLIC_ILD used TMVA
		(-0.8, 0)		25%	
arXiv:0911.0006 [physics.ins-det]	250 GeV	(-0.8, +0.3)	250 fb ⁻¹	91%	ILC/SiD $M_h = 120$ GeV

ILC Running Scenario

optimized scenario with considering

- Higgs precise measurements
- Top physics
- New physics search

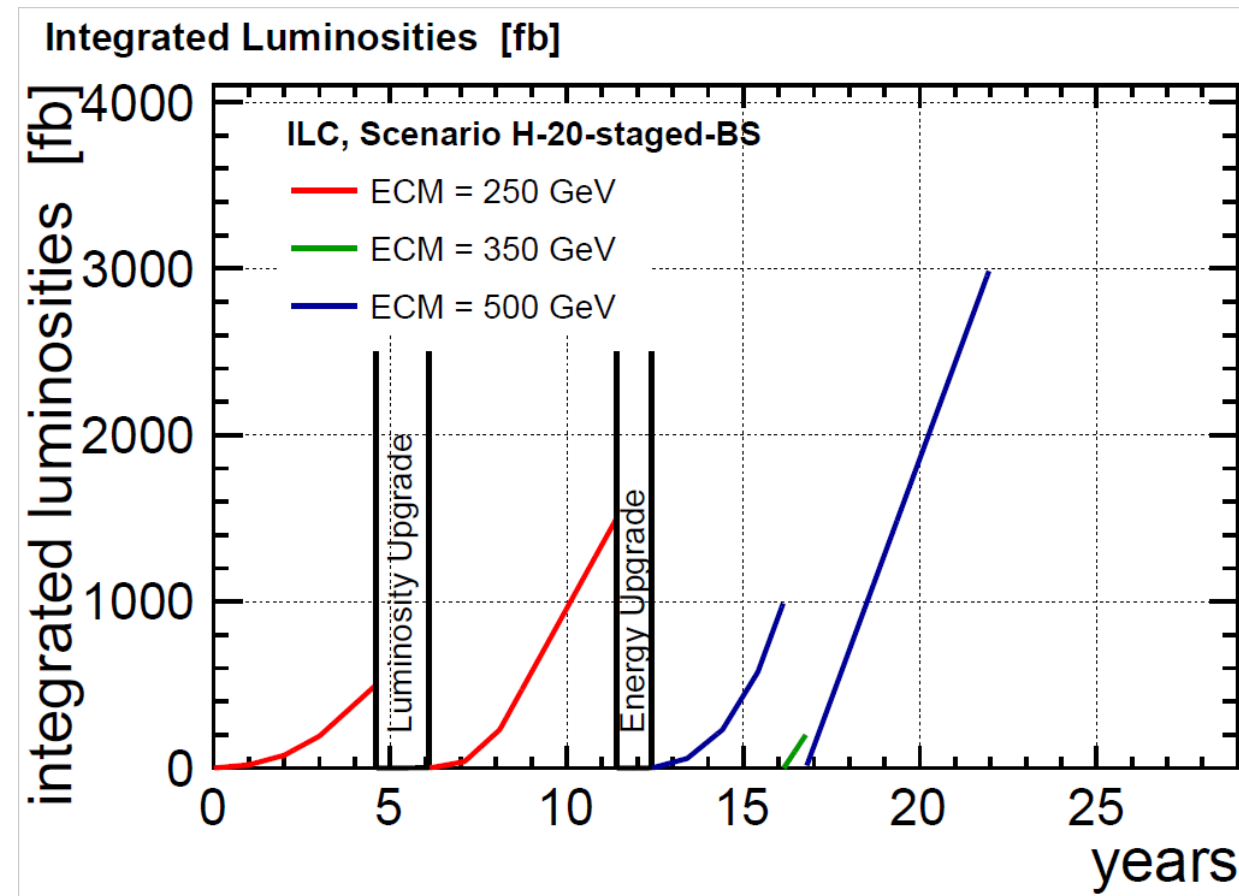
~20 years running with
energy range [250-500] GeV,
beam polarization sharing
---> then possible 1 TeV upgrade

preferred scenario:

2000 fb⁻¹ @ 250 GeV

200 fb⁻¹ @ 350 GeV

4000 fb⁻¹ @ 500 GeV



staging running scenario

Single Higgs Production

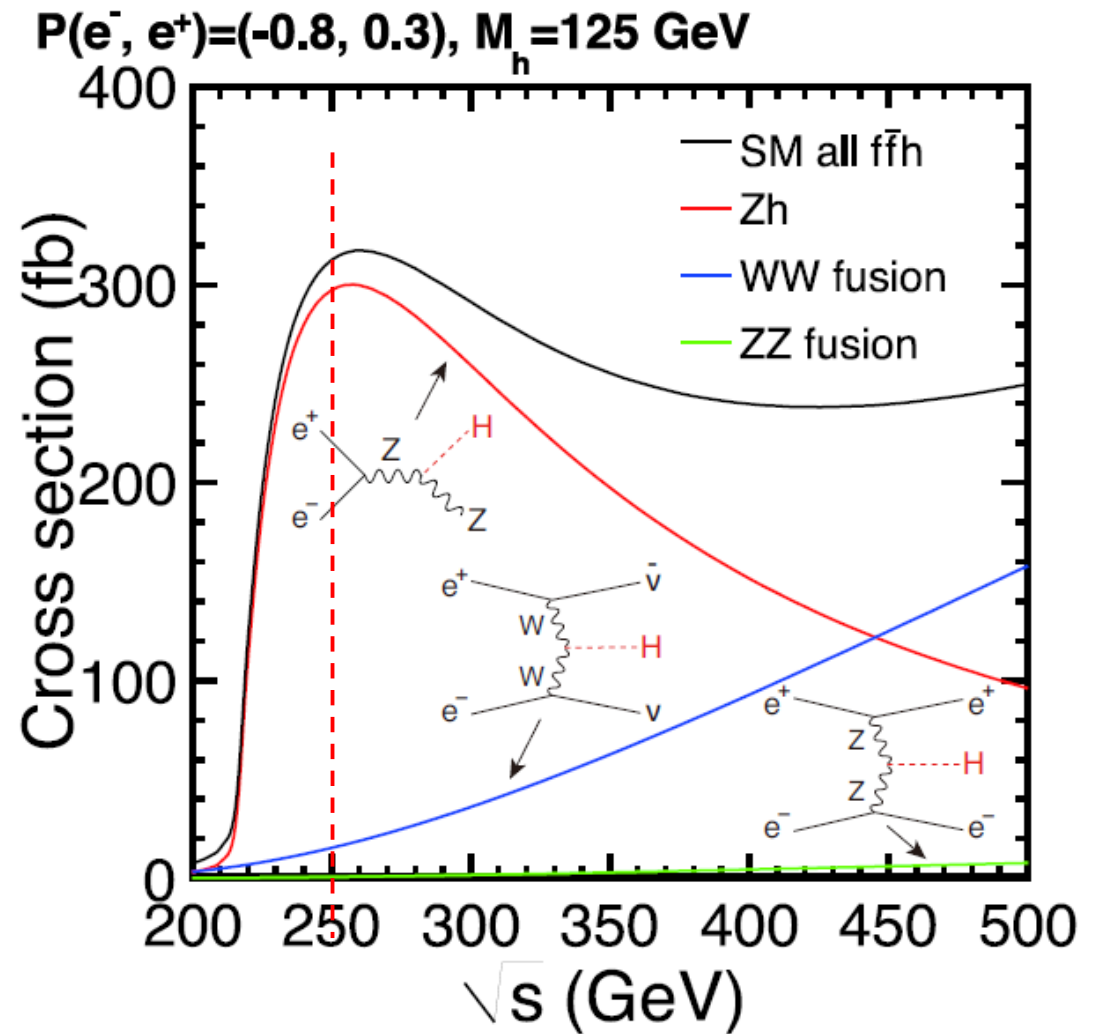
$$\sqrt{s} = 250 \text{ GeV}$$

Higgs-strahlung (Zh) dominant

$$\sqrt{s} = 500 \text{ GeV}$$

WW-fusion dominant

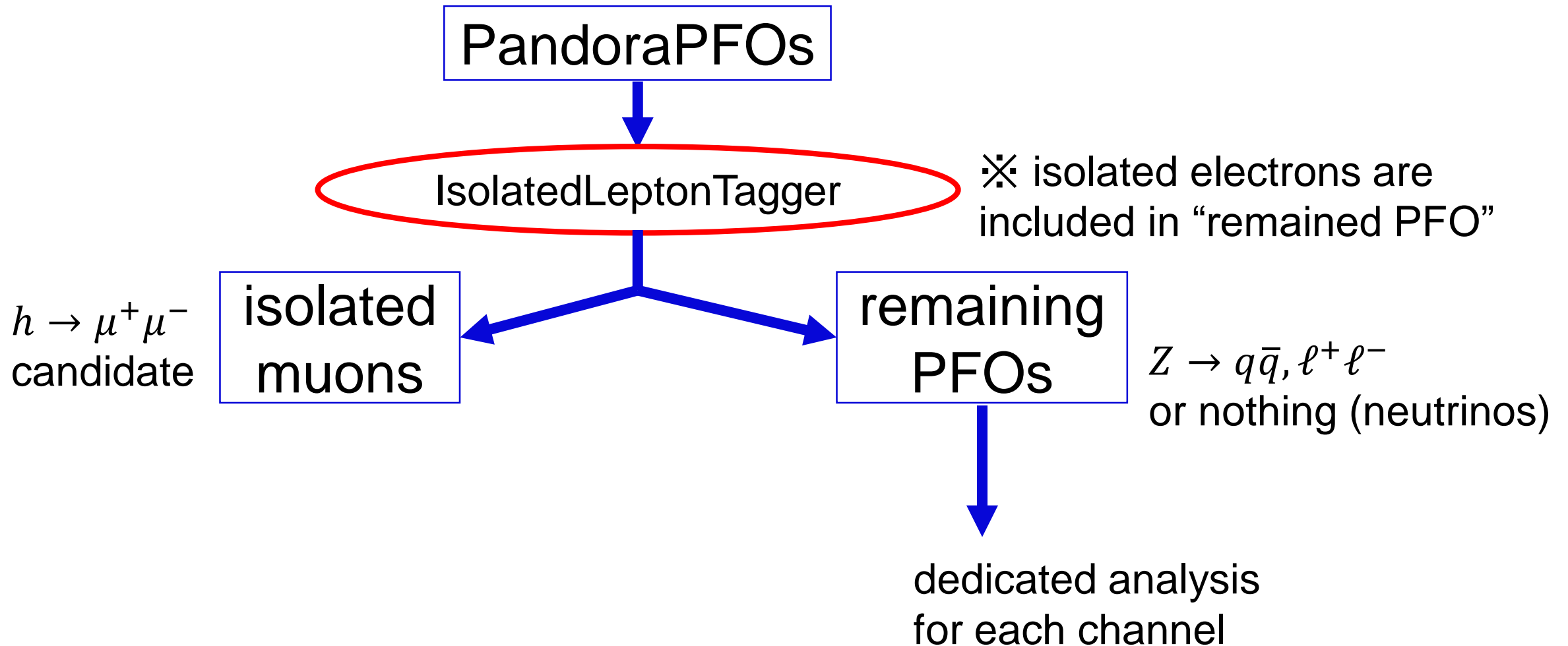
E_{CM}	process	beam pol.	$\int L dt \text{ (fb}^{-1}\text{)}$	# events
500	$\nu\bar{\nu}h$	L	1600	58
		R	1600	8
	$q\bar{q}h$	L	1600	25
		R	1600	16
250	$\nu\bar{\nu}h$	L	900	15
		R	900	8
	$q\bar{q}h$	L	900	41
		R	900	28



L: $(e^-, e^+) = (-0.8, +0.3)$

R: $(e^-, e^+) = (+0.8, -0.3)$

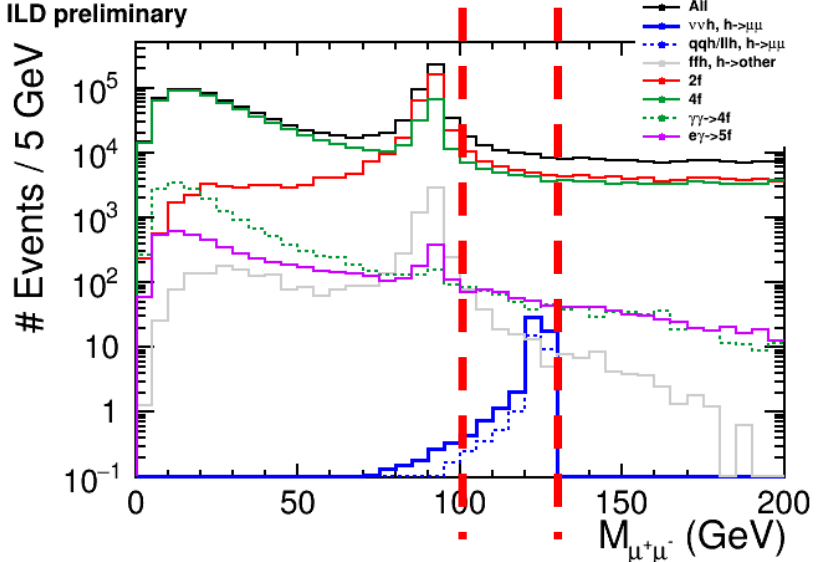
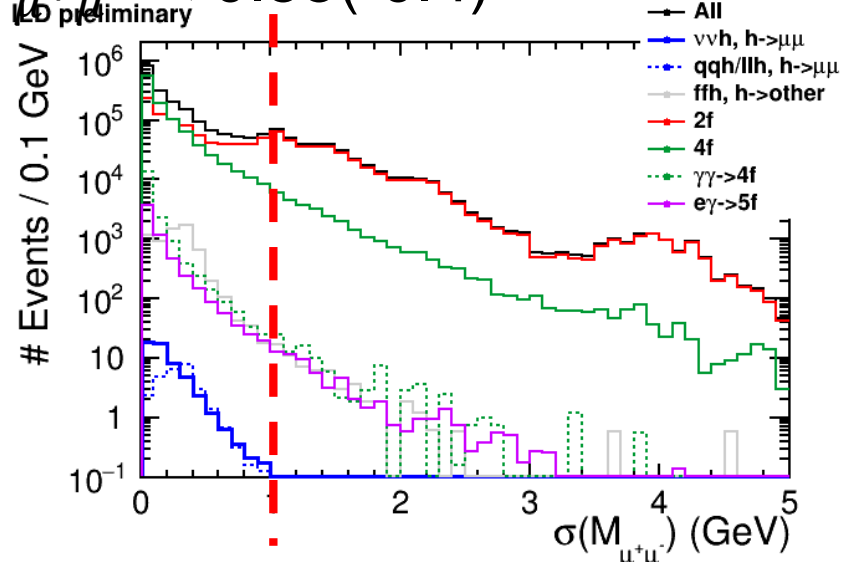
General Event Reconstruction



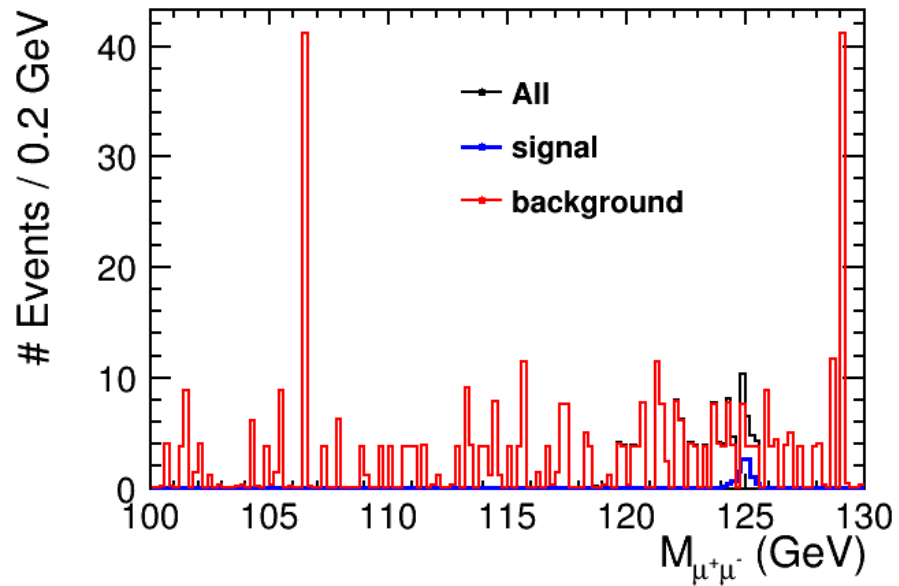
General Event Selection

Selections at 500(250) GeV:

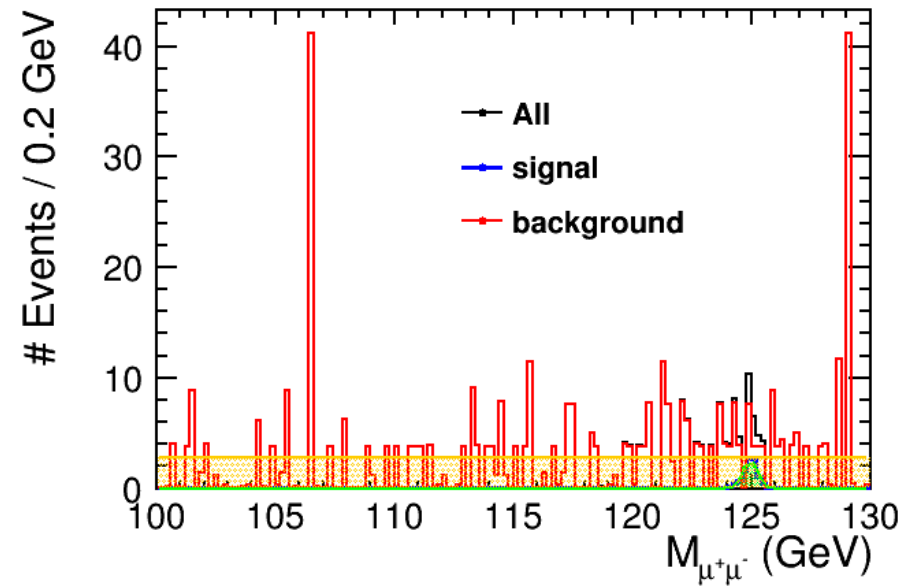
- $\# \mu^+ == 1, \# \mu^- == 1$
- $0.5 < \chi^2(\mu^\pm)/Ndf < 1.5 \longrightarrow$ only select well-measured tracks
- $\sigma(M_{\mu^+\mu^-}) < 1(0.5) \text{ GeV} \longrightarrow$ only select well-measured muon pair
- $|d_0(\mu^\pm)| < 0.02 \text{ mm}, |d_0(\mu^-) - d_0(\mu^+)| < 0.02 \text{ mm}$
- $|z_0(\mu^\pm)| < 0.5 \text{ mm}, |z_0(\mu^-) - z_0(\mu^+)| < 0.5 \text{ mm}$ } only select prompt muons
- $100 < M_{\mu^+\mu^-} < 130 \text{ GeV} \longrightarrow h \rightarrow \mu^+\mu^-$ candidate
- $\cos \theta_{\mu^+\mu^-} < 0.55(-0.4)$



Toy MC Study (1)

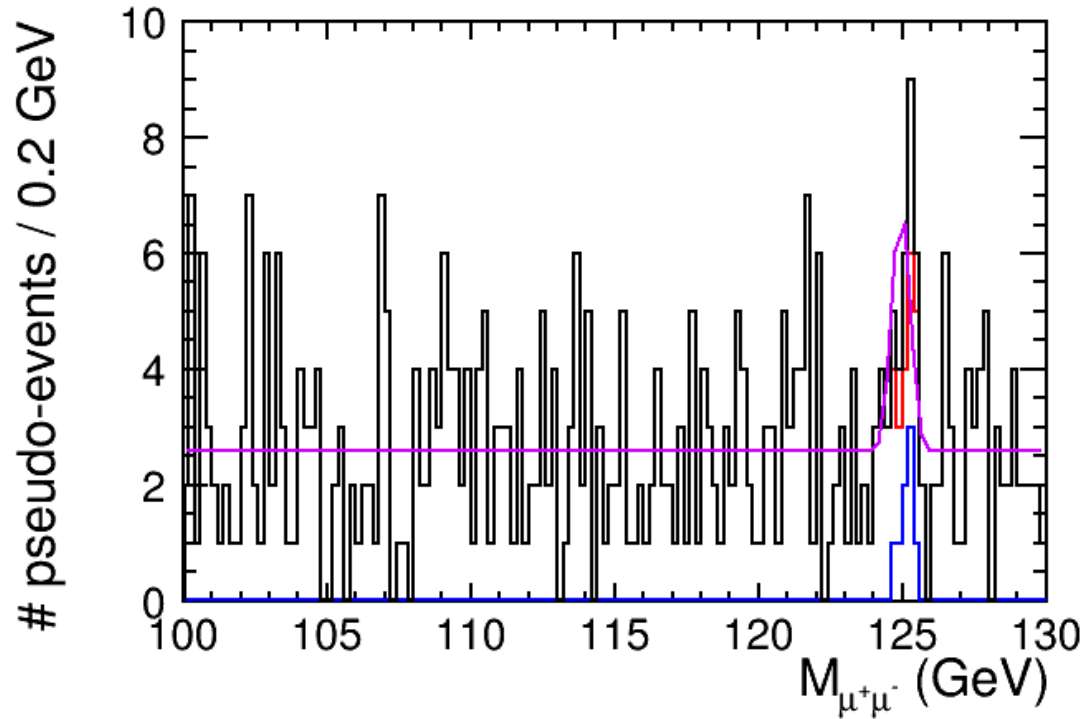


$M_{\mu^+\mu^-}$ spectrum after all cuts
 spiky due to low MC statistics



fitting for toy MC
 f_S : normalized Gaussian (green)
 f_B : constant (yellow)

Toy MC Study (2)



pseudo experiment

blue: signal pseudo data

red: background pseudo data

black = blue + red

purple: result of fit with $f = Y_S f_S + Y_B f_B$

normalization considered

(1) both Y_S and Y_B free

(2) fix Y_B , Y_S is free

repeat 200000 times

obtain Y_S distribution

For Further Improvement

- ISR study (especially qqh and high energy case)
- Pseudomass for nnh
 - Used in OPAL experiment (EPJC **26**, 321-330 (2003))
 - Determine W mass in $W^+W^- \rightarrow \ell^+ \nu \ell^- \bar{\nu}$ process

$$M_{\pm}^2 = \frac{2}{|\vec{p}_{\ell'} + \vec{p}_{\ell}|^2} \left[(P\vec{p}_{\ell'} - Q\vec{p}_{\ell})(\vec{p}_{\ell'} + \vec{p}_{\ell}) \pm \sqrt{|\vec{p}_{\ell'} \times \vec{p}_{\ell}|^2 \{ |\vec{p}_{\ell'} + \vec{p}_{\ell}|^2 (E_{\text{beam}} - E_{\ell})^2 - (P + Q)^2 \}} \right]$$

$$P \equiv E_{\text{beam}}E_{\ell} - E_{\ell}^2 + \frac{1}{2}m_{\ell}^2$$

$$Q \equiv -E_{\text{beam}}E_{\ell'} - \vec{p}_{\ell'} \cdot \vec{p}_{\ell} + \frac{1}{2}m_{\ell'}^2$$

M_+ is sensitive to M_W

ILD preliminary

